

数学 I 休校中の課題解答

教科書P.10[練習9]

- 解答 (1) $8a^5$ (2) $-6x^5y^3$ (3) $-27x^6y^3$

(解説)

(1) $2a^3 \times 4a^2 = (2 \times 4) \times a^{3+2} = 8a^5$
(2) $3x^2y \times (-2x^3y^2) = [3 \times (-2)] \times x^{2+3} \times y^{1+2} = -6x^5y^3$
(3) $(-3x^2y)^3 = (-3)^3 \times (x^2)^3 \times y^3 = -27x^6y^3$

教科書P.11[練習10]

- 解答 (1) $8x^4 - 12x^3 + 20x^2$ (2) $8x^3 - 4x^2 + 6x - 3$ (3) $2x^3 - 3x^2 - 5x + 6$
(4) $2x^4 - 8x^3 + x^2 - 12x - 3$

(解説)

(1) $4x^2(2x^2 - 3x + 5) = 4x^2 \cdot 2x^2 + 4x^2 \cdot (-3x) + 4x^2 \cdot 5$
 $= 8x^4 - 12x^3 + 20x^2$
(2) $(2x - 1)(4x^2 + 3) = (2x - 1) \cdot 4x^2 + (2x - 1) \cdot 3$
 $= 8x^3 - 4x^2 + 6x - 3$
(3) $(2x^2 + x - 3)(x - 2) = (2x^2 + x - 3)x + (2x^2 + x - 3) \cdot (-2)$
 $= 2x^3 + x^2 - 3x - 4x^2 - 2x + 6$
 $= 2x^3 - 3x^2 - 5x + 6$
(4) $(2x^2 + 3)(x^2 - 4x - 1) = (2x^2 + 3)x^2 + (2x^2 + 3) \cdot (-4x) + (2x^2 + 3) \cdot (-1)$
 $= 2x^4 + 3x^2 - 8x^3 - 12x - 2x^2 - 3$
 $= 2x^4 - 8x^3 + x^2 - 12x - 3$

教科書P.12[練習12]

- 解答 (1) $4x^2 + 20x + 25$ (2) $4x^2 - 12xy + 9y^2$ (3) $25x^2 - 16y^2$
(4) $x^2 + 6x + 5$ (5) $x^2 + 5x - 24$ (6) $x^2 - 5xy + 4y^2$

(解説)

(1) $(2x + 5)^2 = (2x)^2 + 2 \cdot 2x \cdot 5 + 5^2 = 4x^2 + 20x + 25$
(2) $(2x - 3y)^2 = (2x)^2 - 2 \cdot 2x \cdot 3y + (3y)^2 = 4x^2 - 12xy + 9y^2$
(3) $(5x + 4y)(5x - 4y) = (5x)^2 - (4y)^2 = 25x^2 - 16y^2$
(4) $(x + 1)(x + 5) = x^2 + (1 + 5)x + 1 \cdot 5 = x^2 + 6x + 5$
(5) $(x - 3)(x + 8) = x^2 + (-3 + 8)x + (-3) \cdot 8 = x^2 + 5x - 24$
(6) $(x - y)(x - 4y) = x^2 + (-y - 4y)x + (-y) \cdot (-4y) = x^2 - 5xy + 4y^2$

教科書P.12[練習13]

- 解答 (1) $8x^2 + 14x + 5$ (2) $2x^2 + 5x - 12$ (3) $3x^2 - x - 14$
(4) $4x^2 - 12x + 5$ (5) $2x^2 + 5xy - 3y^2$ (6) $12x^2 - 17ax + 6a^2$

(解説)

(1) $(2x + 1)(4x + 5) = 2 \cdot 4x^2 + (2 \cdot 5 + 1 \cdot 4)x + 1 \cdot 5$
 $= 8x^2 + 14x + 5$
(2) $(x + 4)(2x - 3) = 1 \cdot 2x^2 + \{1 \cdot (-3) + 4 \cdot 2\}x + 4 \cdot (-3)$
 $= 2x^2 + 5x - 12$

$$(3) (3x-7)(x+2) = 3 \cdot 1x^2 + \{3 \cdot 2 + (-7) \cdot 1\}x + (-7) \cdot 2 \\ = 3x^2 - x - 14$$

$$(4) (2x-5)(2x-1) = 2 \cdot 2x^2 + \{2 \cdot (-1) + (-5) \cdot 2\}x + (-5) \cdot (-1) \\ = 4x^2 - 12x + 5$$

$$(5) (x+3y)(2x-y) = 1 \cdot 2x^2 + \{1 \cdot (-1) + 3 \cdot 2\}xy + 3 \cdot (-1)y^2 \\ = 2x^2 + 5xy - 3y^2$$

$$(6) (3x-2a)(4x-3a) = 3 \cdot 4x^2 + \{3 \cdot (-3) + (-2) \cdot 4\}ax + (-2) \cdot (-3)a^2 \\ = 12x^2 - 17ax + 6a^2$$

教科書P.14[練習16]

解答 (1) $4x^2(3x-2y)$ (2) $ax(3a+6x+1)$

(解説)

$$(1) 12x^3 - 8x^2y = 4x^2(3x-2y)$$

$$(2) 3a^2x + 6ax^2 + ax = ax(3a+6x+1)$$

教科書P.14[練習17]

解答 (1) $(a+b)(c+d)$ (2) $(x-2y)(a-b)$

(解説)

$$(1) (a+b)c + d(a+b) = (a+b)(c+d)$$

$$(2) (x-2y)a + (2y-x)b = (x-2y)a - (x-2y)b \\ = (x-2y)(a-b)$$

教科書P.15[練習18]

解答 (1) $(x+5)^2$ (2) $(x-6)^2$ (3) $(x+3y)^2$ (4) $(2a-b)^2$
(5) $(4a+5b)(4a-5b)$ (6) $2(x+3y)(x-3y)$

(解説)

$$(1) x^2 + 10x + 25 = x^2 + 2 \cdot x \cdot 5 + 5^2 = (x+5)^2$$

$$(2) x^2 - 12x + 36 = x^2 - 2 \cdot x \cdot 6 + 6^2 = (x-6)^2$$

$$(3) x^2 + 6xy + 9y^2 = x^2 + 2 \cdot x \cdot 3y + (3y)^2 = (x+3y)^2$$

$$(4) 4a^2 - 4ab + b^2 = (2a)^2 - 2 \cdot 2a \cdot b + b^2 = (2a-b)^2$$

$$(5) 16a^2 - 25b^2 = (4a)^2 - (5b)^2 = (4a+5b)(4a-5b)$$

$$(6) 2x^2 - 18y^2 = 2[x^2 - (3y)^2] = 2(x+3y)(x-3y)$$

教科書P.15[練習19]

解答 (1) $(x+2)(x+6)$ (2) $(x-3)(x-4)$ (3) $(a-4)(a+5)$
(4) $(x+2y)(x+3y)$ (5) $(a-3b)(a-5b)$ (6) $(x+3a)(x-4a)$

(解説)

$$(1) x^2 + 8x + 12 = x^2 + (2+6)x + 2 \cdot 6 = (x+2)(x+6)$$

$$(2) x^2 - 7x + 12 = x^2 + (-3-4)x + (-3) \cdot (-4) = (x-3)(x-4)$$

$$(3) a^2 + a - 20 = a^2 + (-4+5)a + (-4) \cdot 5 = (a-4)(a+5)$$

$$(4) x^2 + 5xy + 6y^2 = x^2 + (2y+3y)x + 2y \cdot 3y = (x+2y)(x+3y)$$

$$(5) a^2 - 8ab + 15b^2 = a^2 + (-3b-5b)a + (-3b) \cdot (-5b) = (a-3b)(a-5b)$$

$$(6) x^2 - ax - 12a^2 = x^2 + (3a-4a)x + 3a \cdot (-4a) = (x+3a)(x-4a)$$